

***SOAR WITH THE COMMON CORE***

# California Common Core Standards

Session 3 of 5: Mathematics

# Mathematics in the Real World

Activity:

Think about the types of mathematics that you do on a daily basis. Take a couple of minutes to make a list.

# What is shifting?

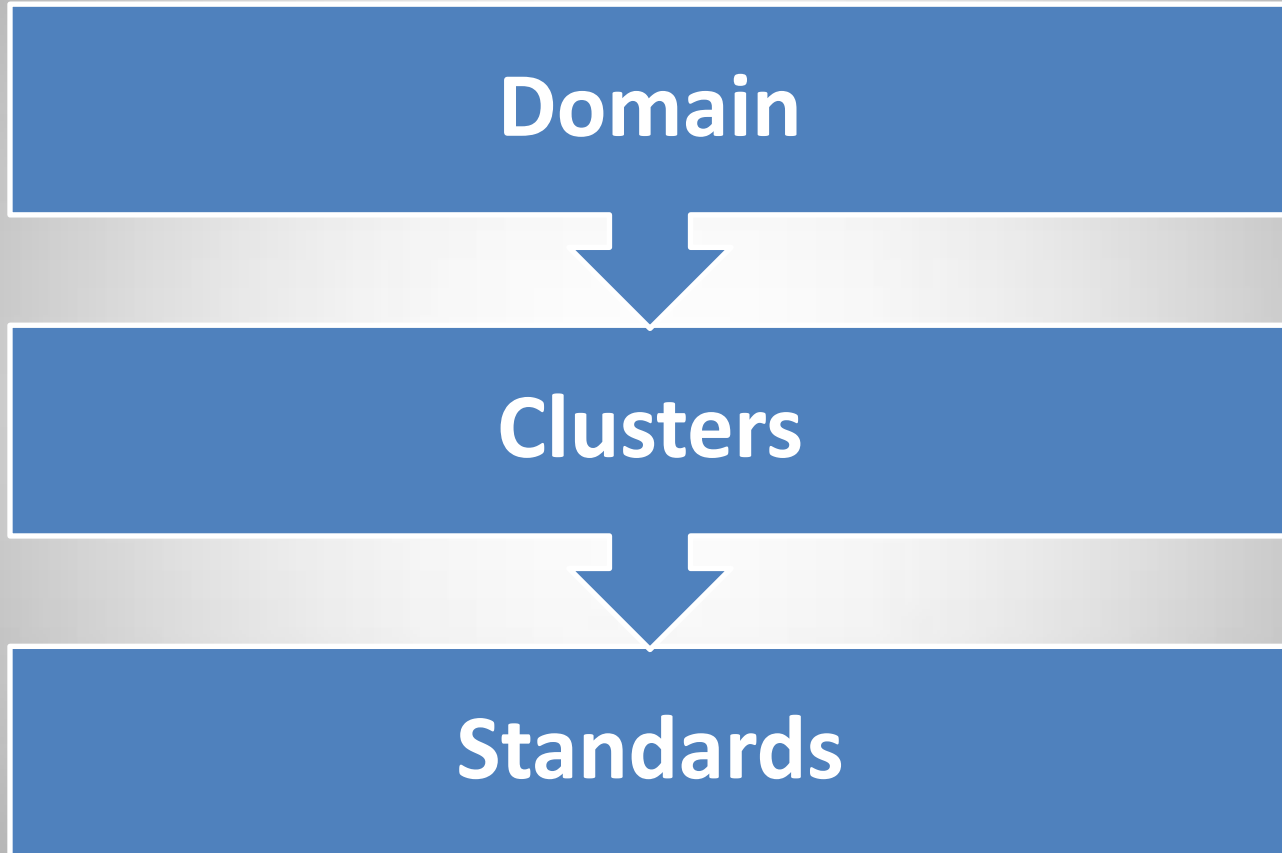
Your child will:

- work more **deeply** with **fewer** topics
- Keep **building** on learning **year after year**
- Spend time practicing **math facts**
- Understand **why** mathematics works and be asked to **talk** about and **prove** their understanding
- Use math in **real-world** situations

The logo for SHIFTS, featuring the word "SHIFTS" in a bold, dark grey sans-serif font. The letter "I" is replaced by two parallel diagonal lines, one blue and one yellow, slanting upwards from left to right.

SHIFTS

# Organization of the Mathematics CCSS



# Organization of the Mathematics CCSS

DOMAIN

## Counting and Cardinality (Kindergarten)

### Know number names and the count sequence

1. Count to 100 by ones and tens
2. Count forward beginning from a given number within the known sequence (instead of having to begin at 1)
3. Write numbers from 0 to 20. Represent a number of objects within a written numeral 0-20 (with 0 representing a count of no objects)

CLUSTER

STANDARDS # 1, 2, 3

# Organization of the Mathematics CCSS

- Two types of standards:

Eight Mathematical Practice Standards

+

Content Standards

**= Habits of Mind**

# Make sense of problems and persevere in solving them.

Mathematical Practice 1



*When presented with a problem, I can make a plan, carry out my plan, and check its success.*

## BEFORE...

**EXPLAIN** the problem to myself.

**MAKE A PLAN** to solve the problem

- What is the question?
- What do I know?
- What do I need to find out?
- What tools/strategies will I use?

## DURING...

**PERSEVERE** (Stick to it!)

**MONITOR** my work

**ASK** myself, "Does this make sense?"

**CHANGE** my plan if it isn't working out

## AFTER...

**CHECK**

- Is my answer correct?
- How do my representations connect to my solution?

**EVALUATE**

- What worked/didn't work?
- How was my solution similar or different from my classmates'?

# Mathematical Practice #1

# Mathematical Practice #2

## Reason abstractly and quantitatively.

Mathematical Practice 2

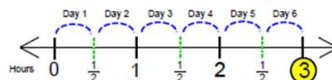


*I can use numbers, words, and reasoning habits to help me make sense of problems.*

**Contextualize** (Numbers to Words)

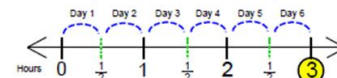
$$\frac{1}{2} \times 6 = 3 \text{ or } 6 \times \frac{1}{2} = 3$$

Mary practices the piano  $\frac{1}{2}$  hour a day for 6 days.  
How many total hours does she practice?



**Decontextualize** (Words to Numbers)

Mary practices the piano  $\frac{1}{2}$  hour a day for 6 days.  
How many total hours does she practice?



$$\frac{1}{2} \times 6 = 3 \text{ or } 6 \times \frac{1}{2} = 3$$

### Reasoning Habits

- 1) Make an understandable representation of the problem.
- 2) Think about the units involved.
- 3) Pay attention to the meaning of the numbers.
- 4) Use the properties of operations or objects.

# Construct viable arguments and critique the reasoning of others.

Mathematical Practice 3



*I can make logical arguments and respond to the mathematical thinking of others.*

I can make and present arguments by...

I can analyze the reasoning of others by...

- using objects, drawings, diagrams and actions
- using examples and non-examples
- relating to contexts

- listening
- asking and answering questions
- comparing strategies and arguments

# Mathematical Practice #3

# Mathematical Practice #4

## Model with mathematics.

Mathematical Practice 4



*I can recognize math in everyday life and use math I know to solve problems.*

I can...

My box turtle is getting a new tank. He is  $5\frac{1}{2}$ " long and 3" tall. One side length of the tank needs to be 5 times his length. How long will the length of the tank need to be?

Use estimates to make the problem simpler.

I will round  $5\frac{1}{2}$ " to 6".

Find important numbers.

**Turtle:** About 6" long  
**Tank:** 5 times the length of the turtle

Consider my **answer** – Does it make sense?  
I thought about the problem again and a 30" side length on the tank makes sense!

Think about the **relationship** to find an **answer**.  
The tank (30") is 5 times bigger than the turtle length (6").

Turtle Length (inches)	Tank Length (inches)
4	20
5	25
6	30
7	35
8	40

Use **tools** to show relationships.

...to solve everyday problems.



# Use appropriate tools strategically.

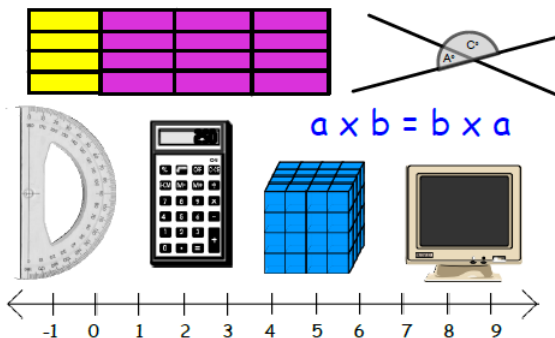
Mathematical Practice 5



*I can use certain tools to help me explore and deepen my math understanding.*

• I know **HOW** and **WHEN** to use math tools.

• I can reason: "Did the tool I used give me an answer that makes sense?"



$$a \times b = b \times a$$

# Mathematical Practice #5

# Attend to precision.

Mathematical practice 6



*I can be precise when solving problems and clear when communicating my ideas.*

Mathematicians communicate with others using...

symbol: equal (the same as)  
48 inches = 4 feet  
↑ units of ↓  
measure

- math vocabulary with clear definitions
- symbols that have meaning
- context labels
- units of measure
- calculations that are accurate and efficient

# Mathematical Practice #6

# Look for and make use of structure.

Mathematical Practice 7



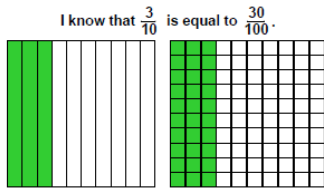
*I can see and understand how numbers and spaces are organized and put together as parts and wholes.*

## Numbers

## Spaces

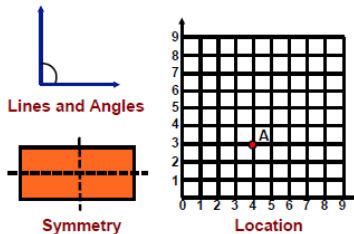
For Example:

For Example:



So,  $\frac{3}{10} + \frac{4}{100} = \frac{34}{100}$ .

Equivalent Fractions



Lines and Angles

Symmetry

Location

# Mathematical Practice #7

# Look for and express regularity in repeated reasoning.

Mathematical Practice 8



*I can notice when calculations are repeated. Then, I can find more general methods and short cuts.*

# Mathematical Practice #8

As I work...

There are many ways to decompose  $\frac{3}{8}$  because it is composed of repeated  $\frac{1}{8}$  s.

I CAN....

...I think about what I'm trying to figure out while I pay attention to the details

....draw a whole and shade in three  $\frac{1}{8}$  s parts.



....add eighths.

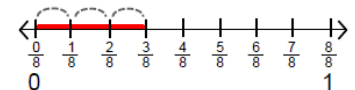
$$\frac{3}{8} = \frac{1}{8} + \frac{1}{8} + \frac{1}{8}$$

....count by eighths. (one-eighth, two eighths, three eighths)

$$\frac{3}{8} = \frac{1}{8}, \frac{1}{8}, \frac{1}{8}$$

...I evaluate if my results are reasonable.

....jump three  $\frac{1}{8}$  size jumps on a number line.

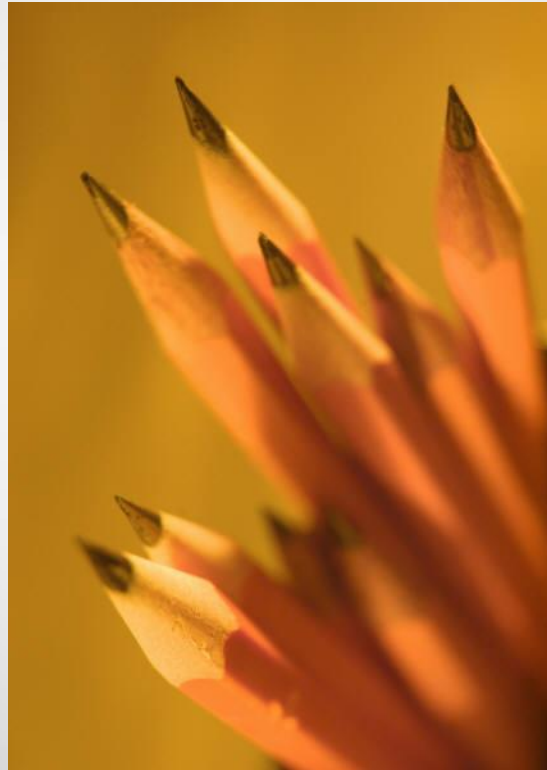


# Let's do some math!

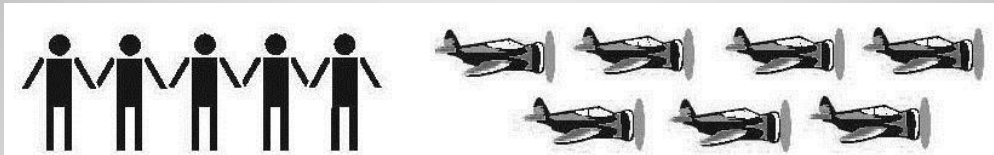
- There are 6 tables in Mrs. Potter's art classroom. There are 4 students sitting at each table. Each student has a box of 10 colored pencils.
  - (A) How many colored pencils are at each table?
  - (B) How many colored pencils do Mrs. Potter's students have in total?

# Standards and Solutions

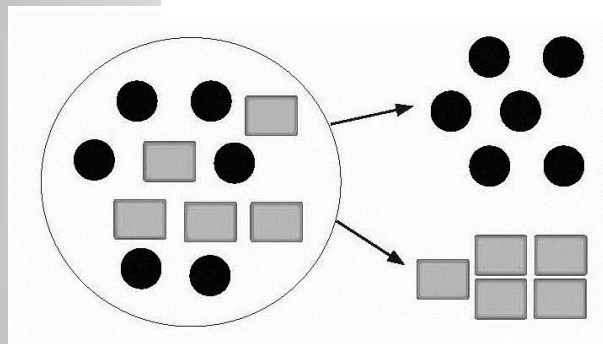
(click on the picture)



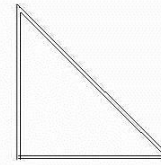
# Content Standards - Kindergarten



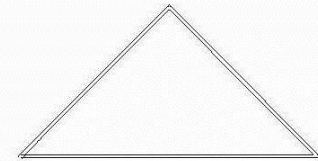
Which group has more? Which group has less?  
Are these groups equal?



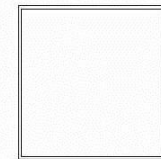
- Count to 100
- Write 0 – 20
- Add and subtract within 5
- Time



(a)



(b)



(c)

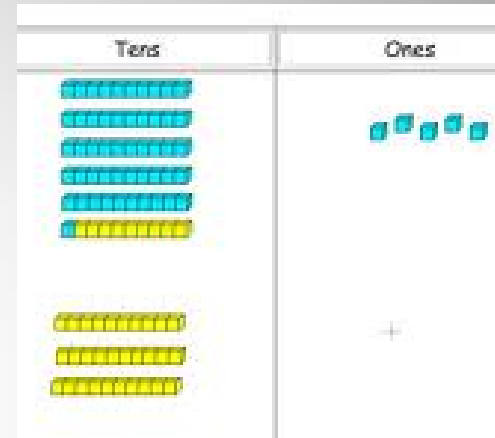
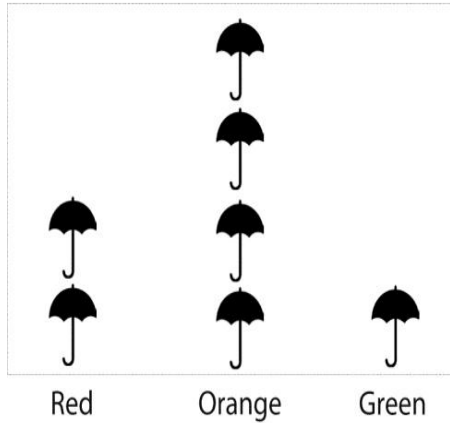


(d)

How many sides and corners do these shapes have?  
Which shape has sides of equal length?

# Content Standards – 1<sup>st</sup> Grade

What color is your umbrella?



What is the most popular color of umbrella? What is the least popular color of umbrella?

If you know  $8+3=11$ , then you know  $3+8=11$

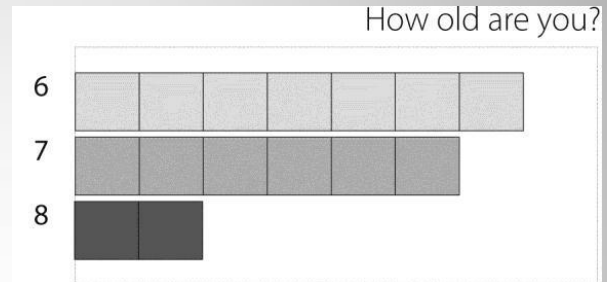
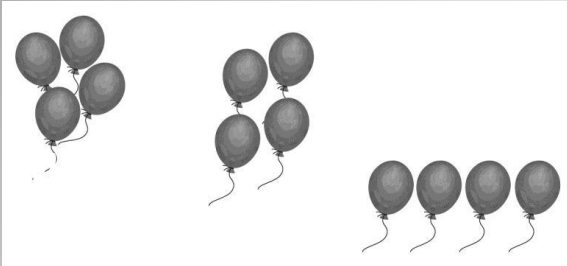


What time is it?



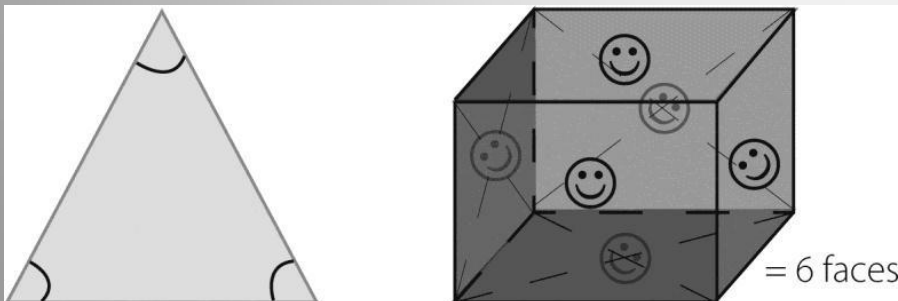
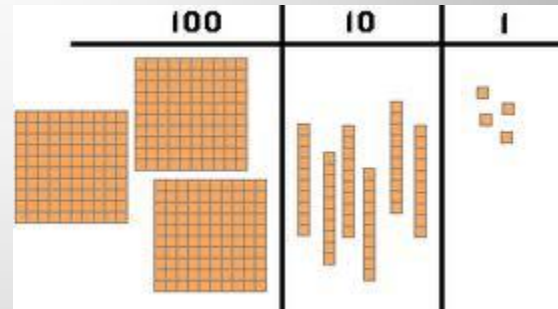
How long is the comb?

# Content Standards – 2<sup>nd</sup> Grade

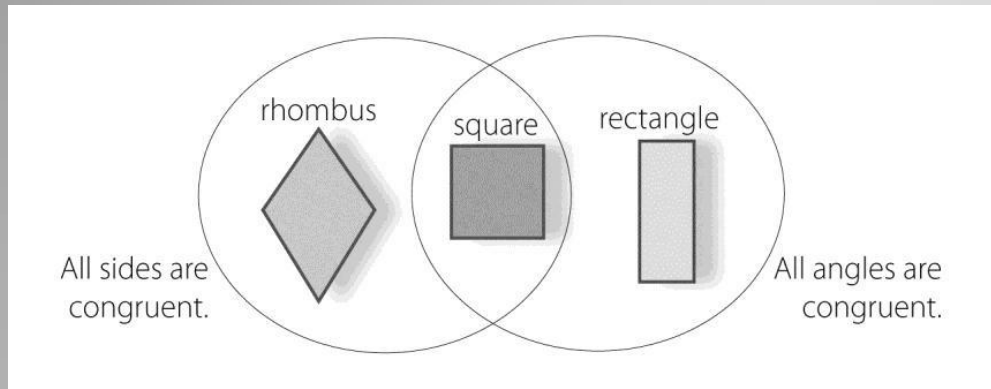


What is the most common age in our class?

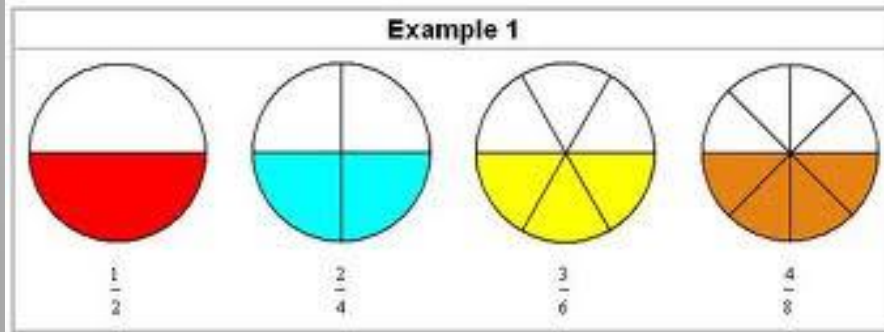
What is the least common age in our class?



# Content Standards – 3<sup>rd</sup> Grade



What do the fractions in example 1 have in common?



**$26 \times 24$**

Sandy walks 26 miles in a month.  
If she were consistent  
in her walking for 2 years, how many  
miles will she have walked?

## Distributive property of multiplication

$$\begin{aligned} \text{If } 8 \times 5 &= 40 \\ \text{And } 8 \times 2 &= 16, \\ \text{Then } 8 \times 7 &\text{ is:} \\ 8 \times (5 + 2) \\ (8 \times 5) + (8 \times 2) \\ 40 + 16 &= 56 \end{aligned}$$

16 cookies are shared equally  
between 4 boys. How many  
cookies will each boy get?

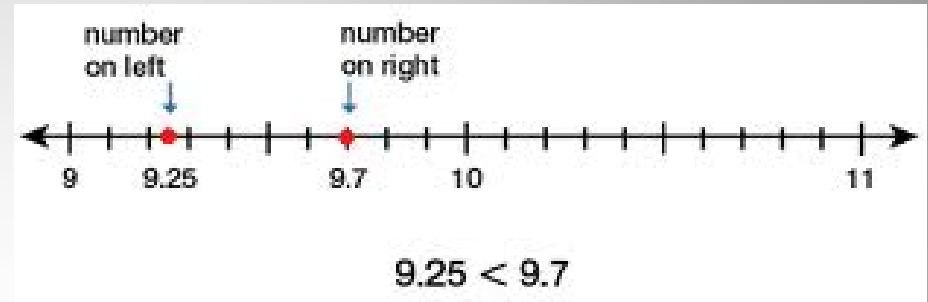
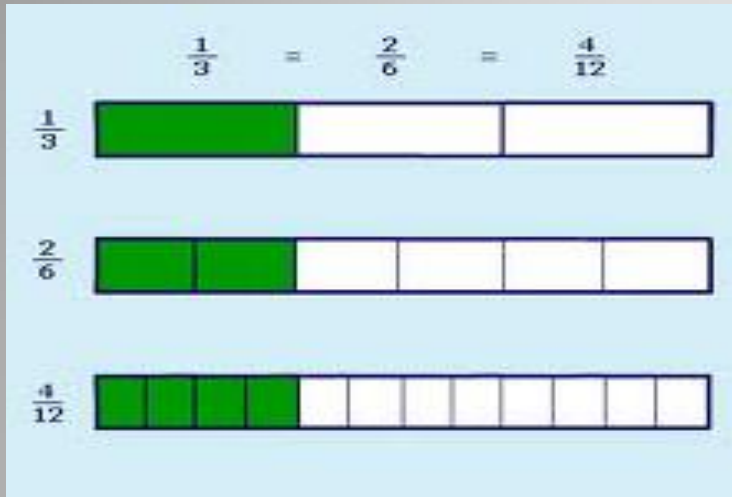
Solution

$$16 \div 4 = 4$$

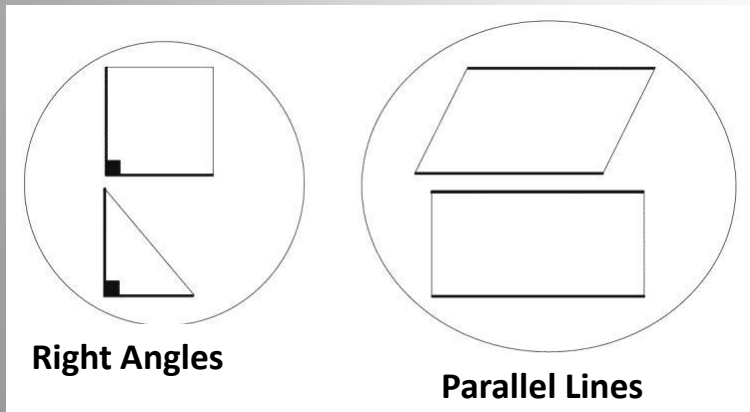
Each boy will get 4 cookies.



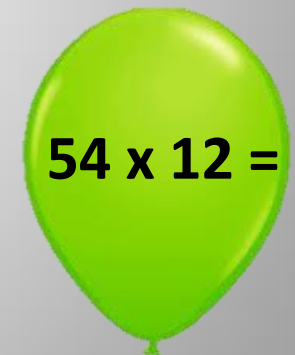
# Content Standard – 4<sup>th</sup> Grade



Expanded form:  $6738 = 6000 + 700 + 80 + 3$

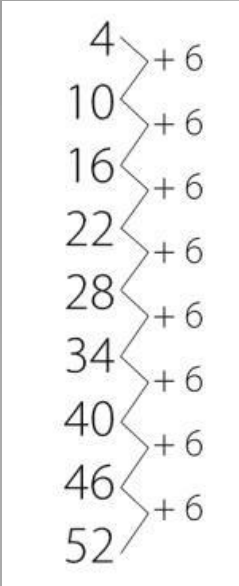


$$\frac{53}{100} = 0.53$$



$$28 \div 7 = ?$$

# Content Standards – 5<sup>th</sup> Grade

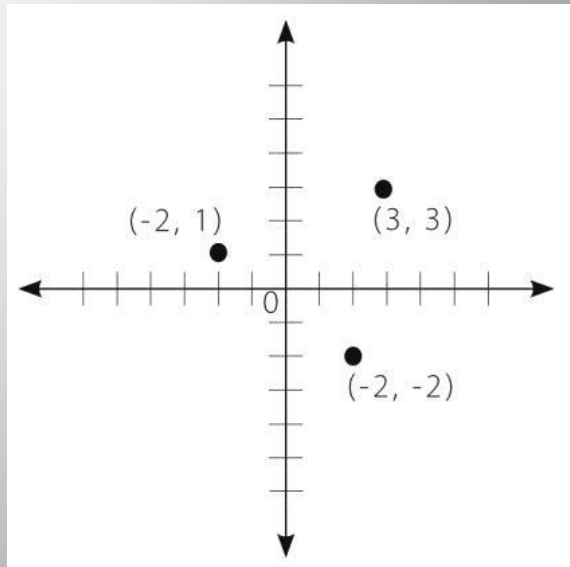
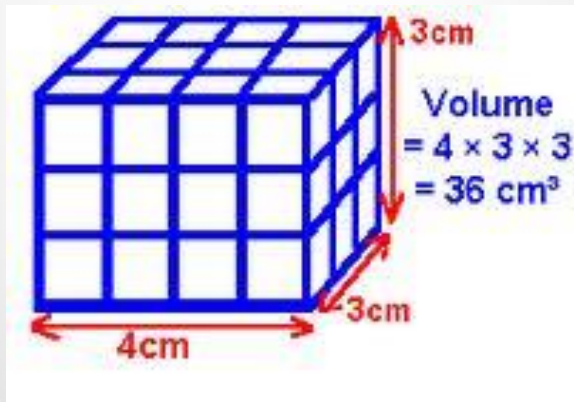


$$\begin{array}{r} 423.12 \\ \times 8 \\ \hline \end{array}$$

$$\begin{array}{r} 8943.43 \\ +17.50 \\ \hline \end{array}$$

$$5 \overline{) 25.75}$$

$$100 - 42.11 =$$



$$\frac{2}{3} \div 3 = \underline{\quad}$$



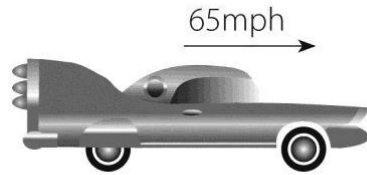
$\frac{2}{3}$  is 3 groups of what number?

# Content Standards – 6<sup>th</sup> Grade

For example, a car travels at a constant speed of 65 mph. List and graph ordered pairs of distances and times. Write the equation  $d = 65t$  to show distance travelled (d) depends on the constant speed (65) multiplied by the time travelled.

$$d = 65t$$

t=hours	distance
1	65
2	130
1/2	32.5

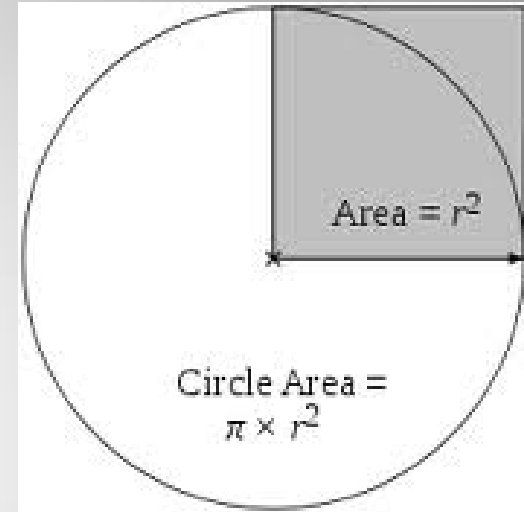


Step 1:  $k \div 3 = 4$

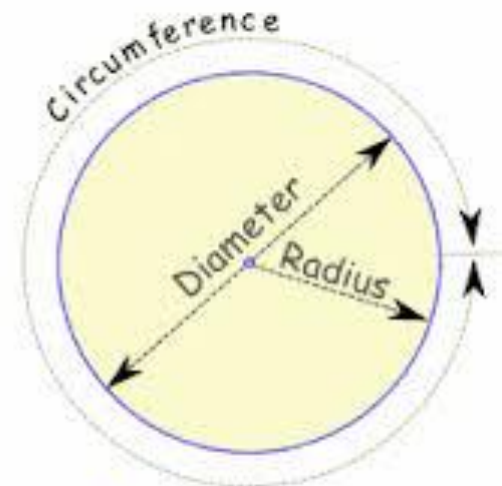
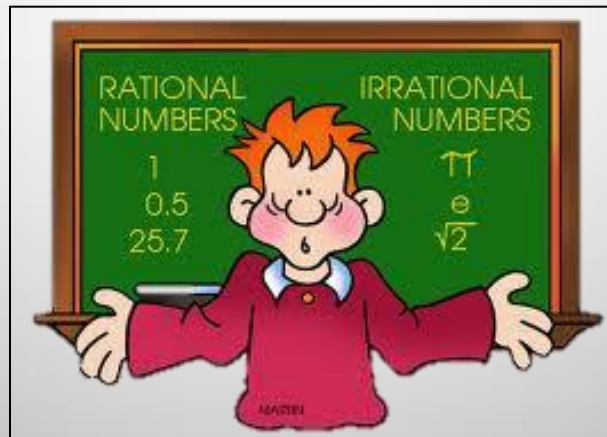
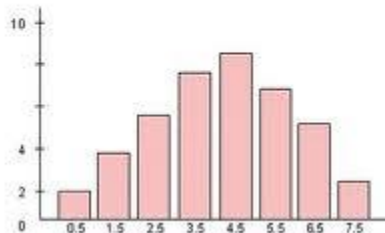
Step 2:  $k \div 3 = 4$   
 $\times 3 \quad \times 3$

Step 3:  $k \div 3 = 4 \times 3$   
 $\times 3 \quad 12$

Step 4:  $k = 12$



HISTOGRAM SAMPLE



$$\frac{\text{Circumference}}{\text{Diameter}} = \pi = 3.14159..$$

# Content Standard – 7<sup>th</sup> Grade

$$6 \times 6 = 6^2 = 36$$

$$\sqrt{36} = 6$$

$$3x - 2(-2x + 7) = -7$$

$$3x + 4x - 14 = -7$$

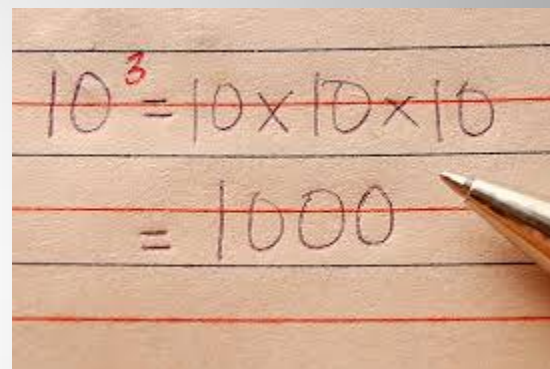
$$7x - 14 = -7$$

$$7x - 14 + 14 = -7 + 14$$

$$7x = 7$$

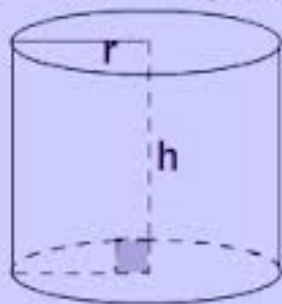
$$\frac{7x}{7} = \frac{7}{7}$$

$$x = 1$$

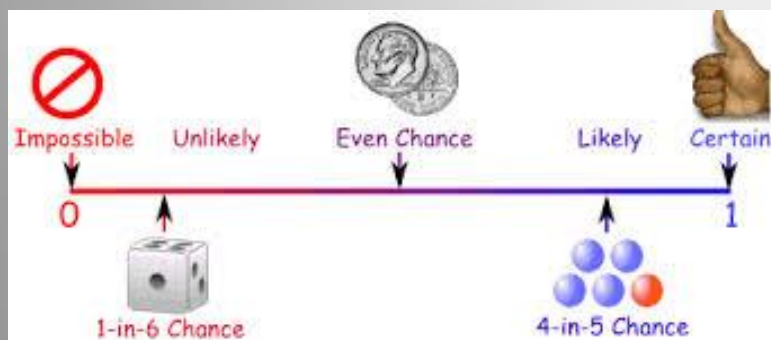


$10^3 = 10 \times 10 \times 10$   
 $= 1000$

$$A = 2\pi r^2 + h(2\pi r)$$



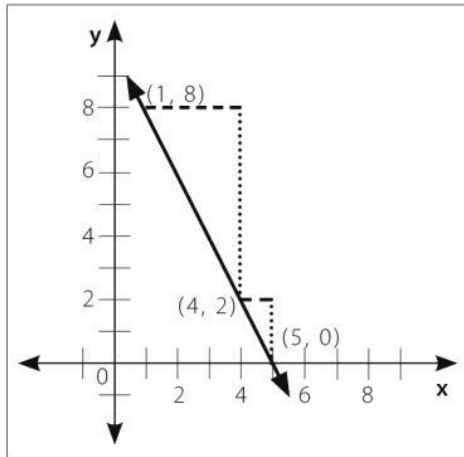
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$$\sqrt[3]{8} = 2$$

# Content Standards – 8<sup>th</sup> Grade

The simplified ratio of the vertical side length to the horizontal side length of each congruent triangle formed by the slope of a line is equivalent to the absolute value of the slope.



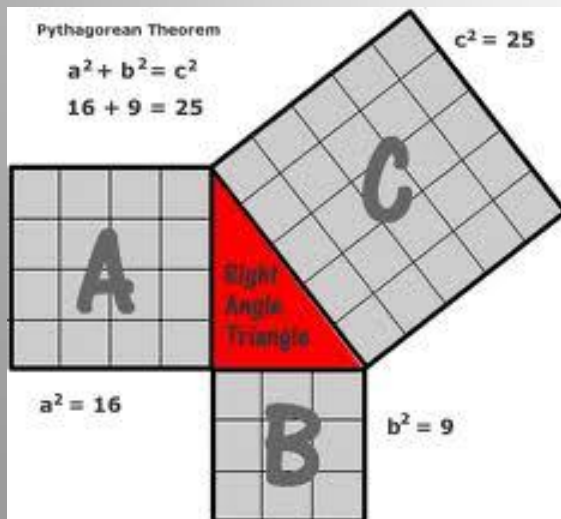
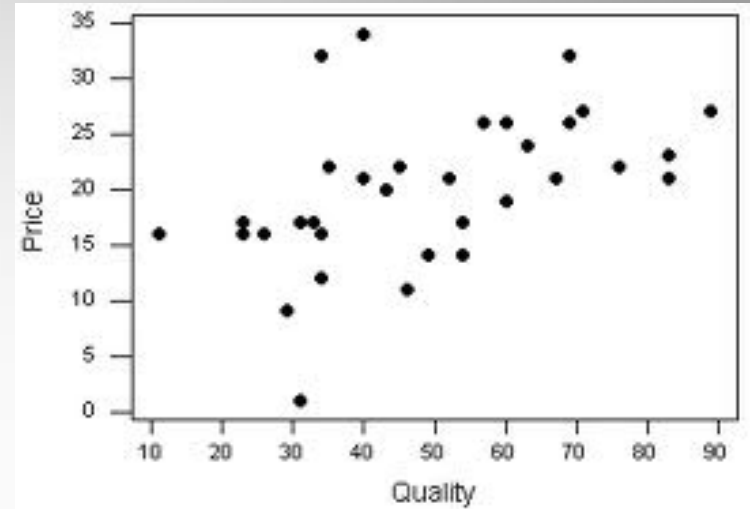
$$\text{slope} = \frac{-2}{1}, \text{ or } -2$$

**Larger Triangle:**

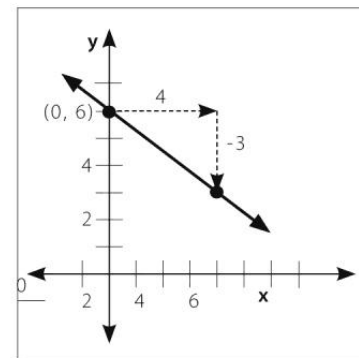
$$\text{ratio: } \frac{\text{vertical side length}}{\text{horizontal side length}} = \frac{6}{3}, \text{ or } 2$$

**Smaller Triangle:**

$$\text{ratio: } \frac{\text{vertical side length}}{\text{horizontal side length}} = \frac{2}{1}, \text{ or } 2$$



Use only the slope and y-intercept to graph  $y = \frac{-3}{4}x + 6$



The slope is  $\frac{-3}{4}$  and the y-intercept is 6.

Since the y-intercept is 6, plot (0,6).

Since the slope is  $\frac{-3}{4}$ , move 4 units to the right of (0, 6) and 3 units down to locate a second point.

Draw the line through the two points.

# Let's do more math!

- You won first place at your school Science Fair!  
You have two choices for the prize:

Option 1: You can take \$20 home with you today.

Option 2: Take \$2 a day for the next 15 days.

1. Which option earns more money? How much more?
2. Which option will you choose? Explain why.

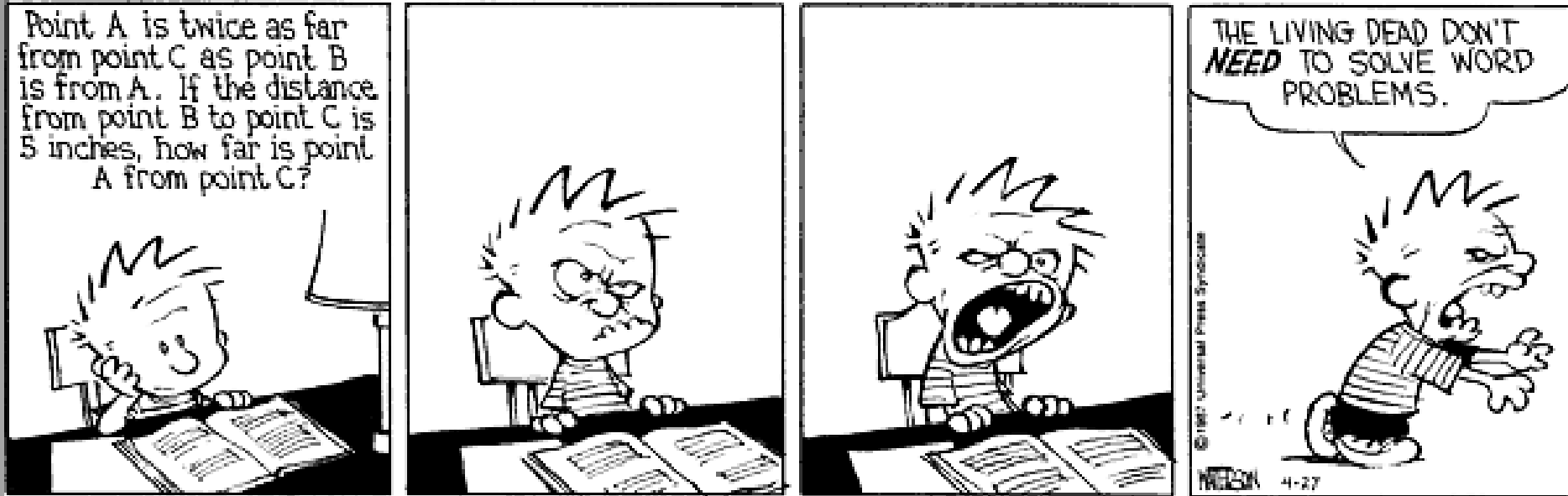


# Standards and Solutions

(click on picture)



# Don't let your child be a Calvin



## How can you help?



# Supporting your Child's Mathematical Learning at Home

- Stay informed about which concepts your child is learning in school.
- Help your child know basic mathematics facts.
- Have your child do the mathematics that pops up in daily life.
- Ask your child's teacher for assistance if something is confusing.
- Ensure that they are doing their homework every day.

*Thank you*

*for*

*joining us today!*